

CROWDFUNDING WITH OVERENTHUSIASTIC INVESTORS: A GLOBAL GAME MODEL

Abstract

Crowdfunding platforms are providing funds to an increasing number of projects, among which many have a strong social/community impact. Under an all-or-nothing program, the success of the investment depends on the ability of a crowd of potential investors to put their funds into the project without an explicit coordination device. With heterogeneous information, such a problem can be analyzed as a typical global game. We assume that signals of at least some agents present a systematic positive bias, driven by positive emotions about projects with high social/community impact. The analysis reveals that if the number of such overenthusiastic persons is large enough, crowdfunding finance might support financially inefficient projects. We then analyze how a monopolistic platform optimally determines transaction fees and unveil the relationship between overenthusiasm and the profit of the platform.

JEL Classification: I11, G23, G41, D83

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1 Introduction

In the last decade, the spectacular development of the Internet has created a myriad of new trading opportunities. In particular, advances in information technology have allowed for the emergence of crowdfunding platforms through which a large number of anonymous small investors, spread all over the world, can fund entrepreneurial projects that might not have benefited from traditional financing mechanisms (Agrawal et al., 2014; Mollick, 2014; Belleflamme et al., 2015). In the US, the Obama Administration JOBS Act of 2012 and the subsequent Security and Exchange Commission rules on May 2016 lifted barriers on equity crowdfunding, which provided further momentum to the industry.¹ A number of platforms specialized in start-up equity finance have recently emerged (CrowdFunder, CircleUp) next to the early generalist platforms such as Kickstarter or Indiegogo. Other platforms manage sector-specific projects; for instance MedStarttr, Health Tech Hatch, RedCrow will select medical investment projects, and Fundrise and RealtyMogul specialize in real estate projects. Data on the market size of the crowdfunding industry are relatively scarce, but equity crowdfunding, where investors expect a direct financial return from their investment, was estimated at 2.5 billion dollars worldwide in 2015 by Crowdexpert, a consulting company.²

The main programs offered by these platforms are of the "all-or-nothing" type: the project will be developed only if the number of contributors who participate to the project allows the entrepreneur to collect a predefined amount of capital that is expected to cover

¹ See: SEC Regulation Crowdfunding <https://www.sec.gov/rules/final/2015/33-9974.pdf>. It states that "Regulation Crowdfunding, among other things, permits individuals to invest in securities-based crowdfunding transactions subject to certain thresholds, limits the amount of money an issuer can raise under the crowdfunding exemption, requires issuers to disclose certain information about their offers, and creates a regulatory framework for the intermediaries that facilitate the crowdfunding transactions."

² See <http://crowdexpert.com/crowdfunding-industry-statistics/>

the development cost. Otherwise, the call for funds is closed, and funds are returned to the backers of the project. Thus, the success of the investment depends on the decision of potential investors to put their money into the project without an explicit coordination device. Hence these markets incorporate a "strategic uncertainty" component that goes beyond the classical financial risk. Depending on the project, the investor's return can be participation in future profits, or merely receiving the future product for free or at a discounted price or in advance of commercial distribution. As emphasized by Belleflamme et al. (2015), non-monetary considerations seem to provide an important motivation for crowdfunding investors regardless of the field. Thus investors' subjective assessment of the final return might be influenced by their positive emotions associated to what they perceive as a meaningful project. Platforms are the first to point out the social impact of these projects. For instance, on their websites, Kickstarter is emphasizing an activity "fully dedicated to building community around creative projects"; Indiegogo will point out a portfolio "loaded with clever and surprising innovations in tech, design, and more"; while MedStartr openly claims to "inspire patients, physicians, and partners to open their wallets by offering smart, fun, and tangible rewards... that can improve healthcare, make people healthier, and solve problems."³

Crowdfunding platforms have attracted the interest of theoretical economists, who are challenged by the rapid and somehow unexpected development of these extremely decentralized investment markets. Agrawal et al. (2014) provide a survey of the early literature, and emphasize the role of crowdfunding platforms in signaling quality, feedback transmission and

³ Extraction on 20/11/2017: www.kickstarter.com/learn?ref=nav; Extraction on 20/11/2017: www.indiegogo.com/about/what-we-do#/funding; Extraction on 23/08/2017 at www.medstartr.com/pages/faqs.

trust facilitation. Several recent papers study crowdfunding as a mechanism design problem and reveal when this type of investment might dominate traditional investment mechanisms (inter alia, Grunner et al., 2015; Ellemenas and Hurkens, 2015; Strausz, 2017). Belleflame et al. (2014) set up a two-stage model of crowdfunding with pre-orders, assuming that investors would also demand the product, and study the optimal reward scheme. Hildebrand et al. (2016) analyze the functioning of Prosper.com, a borrowers/lenders crowdfunding platform, and point out the perverse effects stemming from the asymmetry of information, that ultimately leads to a high default rate.

This paper contributes to this literature by studying investors' coordination problem in these highly decentralized markets, and the optimal decision of a monopolistic platform that can choose the success fee. In our model, entrepreneurial projects are assumed to emerge sequentially; the return of a given project is a draw from a known statistical distribution. Investors observe the true return of any given project with a bias. In the first part of the paper, we analyze the investor decision problem whether to back the project or not, taking as a given the fee chosen by the platform. In the second part, we explain how a monopolistic platform chooses its fees taking into account the response of investors. As the success of the investment depends on many small investors reaching a predetermined investment target, the investor decision problem can be analyzed as a standard coordination game with strategic complementarity. Under perfect information, these games present multiple equilibria (Diamond and Dybvig, 1993). For instance, in our framework, if all investors participate, the investment target is reached, the project is implemented, and each investor will reap a benefit. On the other hand, if all investors choose the risk free asset, an individual who

unilaterally deviates and invest in the project earns nothing. Carlson and van Damme (1993) and Morris and Shin (1998, 2001, 2004) introduced a refinement able to remove the multiplicity of equilibria by making investors' information heterogenous, which provided many applications to capital investment (for a survey, see Jorge and Rocha, 2015 or Angeletos and Rian, 2016). They show that if each investor receives a biased idiosyncratic signal about the true financial performance of the project, investors' beliefs are no longer common knowledge, and the game presents a "threshold equilibrium" characterized by a critical signal above which an investor will participate in the risky project. In equilibrium, this critical signal is determined in conjunction with a cut-off return that ensures the participation of a sufficient mass of investors such as the project can implement.

We extend the traditional analysis to allow for a subset of the population of potential investors to have an overenthusiastic evaluation of the future financial returns of the project. This bias is backed by their positive emotions activated by investing in a "good", socially impactful project. Our modelling assumption is grounded in an extensive literature in psychology and experimental economics, which revealed that, depending on the context, human beings may develop systematic perception and self-perception biases. As an example, a substantial body of literature in corporate finance shows that CEOs tend to overestimate returns from their investments (Malmendier and Tate, 2005), a miscalculation stemming from their overconfidence in their own skills. Bénabou and Tirole (2002, 2016) acknowledge that such belief distortion cannot be discarded by economic analysis, and provide a theoretical framework for understanding these departures from strict rationality. Armstrong and Spiegel (2007) and Grubb (2015) survey the substantial literature that emphasizes cognitive biases

and bounded rationality in consumer choices. In the realm of crowdfunding, Agrawal et al. (2014) point out that "founders and creators are initially overoptimistic about outcomes", and present cases where investors revised downward their expectations when some artists failed to deliver on their musical projects. Davis et al. (2017) analyze the psychological mechanism through which a project pitch perceived as creative fosters chances that the individual will support the project.

Our analysis shows that the presence of these overenthusiastic agents raises the number of participants in the project and the chances that the project is implemented. Furthermore, it can be shown that some of the successful projects might be financially inefficient even if the uncertainty surrounding the project is small, thus bringing a net return that is inferior to the return on the risk free asset. Furthermore, the scope for such inefficiency broadens if the number of overenthusiastic agents increases. In the second part, the analysis reveals a non-monotonic relationship between the success fee charged by the platform and the ex-ante expected profit; we can determine the optimal fee chosen by a monopolistic platform. We further study how the maximum expected profit is related to the frequency of overenthusiastic agents.

The paper is organized as follows. The next section introduces the main assumptions of the model. Section 3 solves the investor decision game for the threshold equilibrium. The properties of the solution are analyzed in section 4. In Section 5, we analyze the optimal choice of the fee by the platform. The last section concludes.

2 Main assumptions

We study the interaction between the crowdfunding platform and a large group of investors.

The supply of entrepreneurial projects is assumed to be exogenous.

At each time period, a new investment project becomes available. Depending on the funding agreement, the return can be participation in the future profit, or the market value of the product if the investor agrees to receive the product as a reward. The actual return θ , to be achieved after the development and commercialization of the product, is a random variable that acknowledges the multiple risks associated with such projects (technological, demand, regulatory). More specifically, we assume that the distribution of net returns is uniform on the support $[0, Z]$, with Z large, $\theta \rightsquigarrow \text{unif}[0, Z]$.⁴ This distribution is common knowledge and will capture the classical financial risk.

There is a continuum $[0, M]$ of potential investors, each being endowed with 1 dollar of savings. They can invest their funds in a risk free asset or invest them in a risky project with the same duration of investment as the risk free asset. To keep the analysis simple, we consider that individuals are risk neutral. Let L denote the number of investors who decide to participate in the entrepreneurial project. The project implies a known development cost V . If enough investors participate ($L \geq V$), they can cover the development cost and the project is implemented; otherwise ($L < V$), the project fails and investors recover their initial funds. To simplify notation, we normalize the mass of investors to 1 and denote by $l = L/M$ the number of investors and denote by $v = V/M$ the investment target. Then the

⁴ This assumption allows us to provide explicit solutions. With normally distributed returns the model can be solved for a graphic solution.

success condition of the project is merely:

$$l \geq v. \tag{1}$$

In general crowdfunding platforms are for-profit organizations. In all-or-nothing campaigns, they charge a fee per dollar invested if the investment target v is met. This success fee is determined by the platform at the outset of the game and is taken as given by investors.⁵

Let ρ denote the success fee.

Thus, the net return of an investor contingent upon his/her decision and the decision of the other investors is:

$$\left\{ \begin{array}{l} \text{invest in the entrepreneurial project:} \\ \text{invest in the safe asset: } r \end{array} \right. \left\{ \begin{array}{l} (\theta - \rho), \text{ if } l \geq v \\ 0 \text{ if } l < v \end{array} \right.$$

Following the standard approach in the global games literature, we assume that when a new project becomes available, each investor makes his subjective evaluation of its potential return, based on his/her own reading of the project, which can differ from the "true" return. As an original development of this paper, we further consider that the set of potential investors comprises two distinct types of players:

- There are $(1 - \gamma)$ "rational agents" who consider the project with a "cold heart" as an ordinary financial investment project. In this subset, each investor i has a personal measure x_i of the project value: $x_i = \theta + \varepsilon_i$, with $\varepsilon_i \rightsquigarrow \text{unif}[-\epsilon, \epsilon]$ and $\epsilon > 0$. In this first group, even if the assessment of the project is imperfect, investors have a globally unbiased evaluation of

⁵ For instance, Kickstarter will charge 5% of the collected funds, Medstart charges 6%. Some transfer charges can also be included.

its return.⁶

- The remaining γ investors are "overenthusiastic". An overenthusiastic investor has a systematic positive bias in the assessment of the returns related to the very nature of the entrepreneurial project. In contrast with the rational investor, his/her signals are: $x_i = \theta + \varepsilon_i + \mu$, where $\varepsilon_i \in [-\epsilon, \epsilon]$ and $\mu > 0$. As explained in the introduction, the bias μ stems from the positive emotions related to an investment in a product with a social dimension, a feeling of "doing good" specific to some humans.

However, we assume that overenthusiastic agents are not aware of their bias; otherwise, they would correct it. Overconfident CEOs do not consider themselves overconfident, and they would not agree that they tend to exaggerate potential returns compared to the benchmark group of CEOs. In the case of crowdfunding investment let's say in arts or the medical sector, those who provide an enthusiastic assessment do not consider themselves enthusiastic, they just do what they have to do. They therefore use the same decision rule as the rational agents.

Regardless of their type, all investors are aware of the presence of overenthusiastic investors as a general characteristic of the market. More specifically, they all know the nature of the assessment bias and the distribution of overenthusiastic investors in the population. Let us denote by l_R (respectively l_O) the frequency of rational (respectively overenthusiastic) investors who decide to participate in the risky project.

The success condition (1) becomes:

$$l = (1 - \gamma)l_R + \gamma l_O \geq v. \tag{2}$$

⁶ This assumption is at the heart of all existing global games.

In the following, the amount of overenthusiasm defined by the product $\omega = \gamma\mu$ plays an important role in the analysis; we will refer to γ as the extensive margin of overenthusiasm and to μ as the intensive margin.

As an upshot of these, the decision timeline is:

$t = 0$	$t = 1$	$t = 2$	$t = 3$	$t = 4$
Platform	Project emerges	Investor i	Investors:	Project:
sets ρ	$\theta \in [0, Z]$	observes x_i	invest/wait	succeeds/fails

Decision Timeline

3 The equilibrium of the investment game

Morris and Shin (1998, 2001, 2004) have shown that such n -person coordination games with heterogeneous information present a "threshold equilibrium" in which all investors receiving a signal above a critical value x^* invest and all those who receive a signal below x^* refrain from investing in the risky project. Connected to this critical signal, there is a cut-off "state variable" θ^* characteristic of the payoff of the successful project above which the project succeeds, and below which the project fails. We follow the now standard resolution steps (Atkeson, 2001; Veldkamp, 2011) and directly determine the two critical thresholds (x^*, θ^*) .

1. The cut-off profit θ^* , taking as given the critical signal x^* .

When a project with performance θ is made available on the platform, rational investors observe signals x_{R_i} in the interval $[(\theta - \epsilon), (\theta + \epsilon)]$, and overenthusiastic ones observe signals x_{O_i} in the interval $[(\theta - \epsilon + \mu), (\theta + \epsilon + \mu)]$. Because agents do not know to what type they belong, they use the same decision rule. More precisely, they have the same critical signal

x^* regardless of their type. The frequency of individuals who invest is given by:

$$l_R = \Pr[x_{R_i} > x^* | \theta] = \frac{1}{2\epsilon}(\theta + \epsilon - x^*) \quad (3)$$

$$l_O = \Pr[x_{O_i} > x^* | \theta] = \frac{1}{2\epsilon}(\theta + \epsilon + \mu - x^*) \quad (4)$$

Note that both l_R and l_O are increasing with θ . The total number of investors is obtained replacing the explicit expressions of l_R and l_O in Eq. (2).

$$l = \frac{1}{2\epsilon}(\theta + \epsilon - x^*) + \frac{1}{2\epsilon}\omega. \quad (5)$$

The presence of overenthusiastic agents increases the number of investors beyond what we would expect with only rational agents and makes it easier to reach the target v . For a given critical signal x^* , there is a cut-off return $\theta = \theta^*$ for which the number of investors is sufficient to cover the development cost. This cut-off return is implicitly defined by $l = v$ or:

$$(x^* - \theta^*) = \omega + \epsilon(1 - 2v) \quad (6)$$

This is the first key equation of the game.

2. The critical signal x^* taking as given the cutoff profit .

The observation of the signal allows investors to update their beliefs about the distribution of returns. Any player i who receives a signal x_i believes that θ is uniformly distributed in the interval $[(x_i - \epsilon), (x_i + \epsilon)]$.⁷

In the continuum of investors, there should be a player who is indifferent between investing in the risk free project or in the risky entrepreneurial project. We have denoted his/her signal

⁷ Recall that overenthusiastic players are not aware of their psychological bias, so they have the same updating rule as the rational ones.

by x^* . To determine x^* , we set the indifference condition:

$$\int_{\theta^*}^{(x^*+\epsilon)} (\theta - \rho) dF(\theta|x^*) = r \quad (7)$$

where the left-hand term indicates the expected net return if the investor chooses the risky project, based on the conditional distribution of $\theta \rightsquigarrow [(x^* - \epsilon), (x^* + \epsilon)]$. For $\theta > \theta^*$, the project succeeds and brings to investors $(\theta - \rho)$. For $\theta < \theta^*$ the project fails. With our uniform distribution, the former condition becomes:

$$\begin{aligned} \frac{1}{2\epsilon} \int_{\theta^*}^{(x^*+\epsilon)} (\theta - \rho) d\theta &= r \\ \frac{1}{2\epsilon} \left\{ \left[\frac{\theta^2}{2} \right]_{\theta^*}^{(x^*+\epsilon)} - [\rho\theta]_{\theta^*}^{(x^*+\epsilon)} \right\} &= r \\ [(x^* + \epsilon) - \theta^*][(x^* + \epsilon) + \theta^* - 2\rho] &= 4\epsilon r \end{aligned} \quad (8)$$

This is the second key equation of the global game.

The solution of the game is the couple (θ^*, x^*) that simultaneously fulfills equations (6) and (8):

$$x^* = \frac{2\epsilon r}{[\omega + 2\epsilon(1 - v)]} + \rho + 0.5\omega - \epsilon v \quad (9)$$

$$\theta^* = \frac{2\epsilon r}{[\omega + 2\epsilon(1 - v)]} + \rho - 0.5\omega - \epsilon(1 - v) \quad (10)$$

Note that all projects with $\theta > \theta^*$ will be implemented. Thus the frequency of successful projects is: $f = 1 - (\theta^*/Z)$.

4 Properties of the solution

4.1 Changes in parameters

In line with intuitive reasoning, the cut-off return θ^* is increasing in v , ρ , and r and is decreasing in ω . The higher the critical number of investors requested for the project to

succeed v , the higher the strategic risk; in this case investors will participate only if the project delivers high returns. If the fee (ρ) required by the platform is too high, the investor benefit is eroded, and only a high return would prompt them to come back. When risk free investments provide higher returns (r), a risky project must present a higher profitability in order to be attractive. Finally, the higher the intensive (γ) and the extensive (μ) margins of overenthusiasm, the higher the participation in the project, which makes more projects appealing, including those with lower returns.

The relationship between θ^* and the amount of signal noise (ϵ) is non-linear. Indeed, the derivative

$$\frac{d\theta^*}{d\epsilon} = \frac{2r\omega}{[\omega + 2\epsilon(1-v)]^2} - (1-v) \quad (11)$$

is negative if the noise is high enough, and vice versa.

$$\frac{d\theta^*}{d\epsilon} < 0 \Leftrightarrow \epsilon > \frac{1}{2(1-v)} \left[\sqrt{\frac{2r\omega}{(1-v)}} - \omega \right] \quad (12)$$

We remark that this condition is always fulfilled if the amount of overoptimism is small enough, more precisely if $\omega < \frac{(1-v)}{2r} \Leftrightarrow \sqrt{\frac{2r\omega}{(1-v)}} - \omega < 0$.

4.2 Financial efficiency analysis

We know that all projects with $\theta > \theta^*$ will attract enough investors to be implemented. If $\theta^* < (\rho + r)$, then, among all the successful projects ($\theta > \theta^*$), we can find financially inefficient projects, characterized by $\theta < (\rho + r)$. Indeed, these projects will pay a net return lower than the risk free rate of return.

The general condition indicating when some financially inefficient projects might be implemented is thus $\theta^* < (\rho + r) \Leftrightarrow (\theta^* - \rho) < r$. It can be shown that both the signal noise

and the amount of overenthusiasm contribute to this outcome.

As shown in the Appendix, the former condition is equivalent to:

$$H = [\omega + 2\epsilon(1 - v)]^2 - 2r(2\epsilon v - \omega) > 0 \text{ with } \omega > 0. \quad (13)$$

The function $H = H(\omega)$ is a convex parable. Calculations (also in the Appendix) show that the roots of $H(\omega) = 0$ are:

$$\omega_{1,2} = -[2\epsilon(1 - v) + r] \pm \sqrt{4r\epsilon + r^2} \quad (14)$$

The function takes positive values for $\omega < \omega_1$ and $\omega > \omega_2$,

Obviously, for $\epsilon > 0$ we have $\omega_1 \leq 0$. Thus condition (13) is fulfilled for:

$$\omega > \omega_2 = -[2\epsilon(1 - v) + r] + \sqrt{4r\epsilon + r^2} \quad (15)$$

Denoting by $\epsilon_0 = \frac{rv}{[(1-v)]^2}$, we can check that $\omega_2 > 0$ for $0 < \epsilon < \epsilon_0$ and $\omega_2 < 0$ for $\epsilon > \epsilon_0$.

Proposition 1 *If the noise of the signal is large ($\epsilon > \epsilon_0$), inefficient projects may be implemented regardless of the number of overenthusiastic agents.*

Proof. For a large noise, $\epsilon > \epsilon_0$, the larger root of $H(\omega) = 0$ is negative, $\omega_2 < 0$. Thus

$H(\omega) > 0, \forall \omega > 0$ which is equivalent to $(\theta^* - \rho) < r$. ■

Proposition 2 *If the noise of the signal is small ($\epsilon < \epsilon_0$), yet the number of overenthusiastic agents is relatively large ($\omega > \omega_2$), then inefficient projects may be implemented.*

Proof. For a small noise, $\epsilon < \epsilon_0$, the larger root of $H(\omega) = 0$ is positive, $\omega_2 > 0$. Then, for

$\omega > \omega_2 \Leftrightarrow H(\omega) > 0 \Leftrightarrow (\theta^* - \rho) < r$. ■

Corollary 3 *If the noise of the signal is small ($\epsilon < \epsilon_0$) and overenthusiasm is limited ($\omega < \omega_2$), then all implemented projects are financially efficient.*

As an upshot of these, a large noise or a large number of overenthusiastic agents raise the chances that inefficient projects might be implemented. In a standard global game with strictly rational agents, a small noise would suffice to ensure financial efficiency, an outcome that is challenged by the presence overenthusiastic agents.

5 The optimal fee of the platform

So far, we have studied investors' decision given the fee decided by the platform at the outset of the game. In this section, we analyze how the platform chooses the optimal fee, taking into account the second-stage response of investors.

To keep the analysis as simple as possible, we assume that the platform is the only provider of crowdfunding services. Its goal is to maximize its profits. There is a fixed operating cost, which we can normalize to zero without loss of generality. Then the total profit for the platform is merely the fee times the number of investors.

Then, the profit-maximizing platform faces a dilemma: If it increases the success fee ρ , all things equal, it would earn more per each dollar invested. However, because a higher fee pushes up the equilibrium signal x^* , less investors will participate in each project, and less projects will be successful, as θ^* also increases. For a very large fee, the expected profit must be zero.⁸

Formally, for any given $\theta \in [0, Z]$, the frequency of investors $l(\theta, x^*(\rho))$ is given by equation (5), evaluated for the equilibrium critical signal $x^* = x^*(\rho)$ as defined in equation (9).

The platform must choose and post ρ before θ is realized. It therefore decide on ρ

⁸ A similar trade-off has been revealed by Peia and Vranceanu (2017) in a model of infrastructure project finance.

based on the ex-ante expected profit, and this expectation must take into account the whole distribution of future returns. Formally, the expression of the expected profit is:

$$\Pi = \rho \int_{\theta^*(\rho)}^Z l(\theta, x^*(\rho)) dF(\theta), \quad (16)$$

an expression in which we acknowledge that the platform can charge the fee only if the project is successful, i.e. for $\theta > \theta^*(\rho)$.

After substituting $l(\theta, x^*(\rho))$, $x^*(\rho)$ and $\theta^*(\rho)$ by their explicit forms, calculations in the Appendix allow us to write the expected profit as a function of the fee ρ :

$$\Pi(\rho) = (2Z\epsilon)^{-1} \rho [0.5(a - \rho) + 2\epsilon v] (a - \rho). \quad (17)$$

where we denoted by $a = Z - \frac{2\epsilon r}{\omega + 2\epsilon(1-v)} + 0.5\omega + \epsilon(1-v) > 0$ or $(Z - \theta^*) = (a - \rho)$.

The function $\Pi(\rho)$ is a standard polynomial of third degree with three solutions: $\rho_1 = 0$, $\rho_2 = a$, $\rho_3 = a + 4\epsilon v$, which can be ordered $\rho_1 < \rho_2 < \rho_3$.

Obviously our problem is defined only for parameter values that ensure that $\theta^* < Z \Leftrightarrow \rho < \rho_2 = a$. In the opposite case where $\rho > \rho_2$, then $\theta^* > Z$, no project will ever be implemented, the market does not exist.

We remark that for $\rho < a$ the expected profit is positive.

Proposition 4 *There is an optimal fee, $\hat{\rho}$, which maximizes the ex-ante expected profit of the platform, with $\hat{\rho} \in [0, \rho_2]$.*

Proof. The problem is defined for $\rho \in [0, \rho_2]$. Calculations in the appendix show that $[d\Pi/d\rho]_{\rho=0} > 0$. Also, we know that $\Pi(0) = \Pi(\rho_2) = 0$. Then the function $\Pi(\rho)$ presents a maximum in the interval $[0, \rho_2]$. The first order condition $d\Pi/d\rho = 0$ defines the optimal fee (see Appendix) as:

$$\hat{\rho} = \frac{2}{3} \left[(a + 2\epsilon v) - \sqrt{(0.5a + 2\epsilon v)^2 - \epsilon v a} \right]. \quad (18)$$

■

We can check that $\hat{\rho} < \rho_2$.

As we mentioned, the presence of overenthusiastic investors seem to be an important distinguishing characteristic of crowdfunding investment. It is interesting to study the impact of this psychological bias on the platform decision.

Proposition 5 *The optimal fee is increasing in the number of overenthusiastic agents.*

Proof. See Appendix for the calculation of the derivative $d\hat{\rho}/d\omega > 0$ ■

Which leads us to our last result:

Proposition 6 *The maximum expected profit is increasing in the number of overenthusiastic agents*

Proof. The maximum expected profit is the product of $\hat{\rho}$, $(a - \hat{\rho})$, and $0.5(a - \hat{\rho}) + 2\epsilon v$. We know $d\hat{\rho}/d\omega > 0$. Next, $(a - \hat{\rho})$ is an increasing function in a , and $da/d\omega > 0$, thus $d(a - \hat{\rho})/d\omega > 0$. The maximum expected profit is increasing in ω . ■

This result suggests that a monopolistic crowdfunding platform might have an interest to over-emphasize the "moral" dimension of the project. This strategic communication would push up the amount of overenthusiasm and ensure higher fees and higher profits.

6 Conclusion

In the last few years equity crowdfunding has become an important mechanism for financing entrepreneurial projects with a strong social and community-oriented dimension. A multitude of internet platforms emerged to match projects with investors. Most of them will run all-or-nothing schemes, where funds are transferred to entrepreneurs only if a predetermined and justified investment target is fulfilled. This paper introduces an analysis of the crowdfunding

market that emphasizes the coordination frictions specific to all-or-nothing financing schemes. In a first step, we analyzed investors decisions, taking as given the fee chosen by the platform. In a second step, we analyze how a monopolistic platform chooses the optimal fee.

Because investors are small and anonymous, the success of the projects relies on their ability to coordinate on the "invest" decision. In this paper, we use the global games refinement introduced by Van Damme (1993) and Morris and Shin (1998, 2001) to solve the model for the "threshold equilibrium", characterized by a critical signal and a cut-off return. As an original contribution of this paper, we allowed for some agents to develop a positive and insidious perception bias, grounded in positive emotions activated by the investment in a meaningful product. Such affect backed bounded rationality can be at work in various crowdfunding projects (Agrawal et al. 2014; Belleflamme et al. 2014; Davis et al. 2017).

Most often, crowdfunding platforms claim to reduce project risk through a careful selection of the best projects by qualified experts. At the same time, they will communicate extensively on the social impact of the project. Our model shows that, by contrast with the insights of a classical global game with strictly rational agents, in the presence of overenthusiastic agents that present a positive perception bias, financially inefficient projects can be implemented even if the precision of the signal is large. Thus, reducing the noise of the signal by expert screening might be offset by an investment behavior guided by positive feelings about the nature of the investment project, which would ultimately lead to implementation of financially inefficient projects and deceive investors.

We also show that the relationship between the fee chosen by a monopolistic platform and the expected profit is non-linear and solve the problem for the profit maximizing fee. This

fee is an increasing function in the number of overenthusiastic agents and so is the expected profit of the platform, despite the negative effect of the higher fee on the total number of investors. This might explain the tendency of existing platforms to over-communicate on the social impact of the product and also might explain why many projects might fail to deliver on their high promises.

In our paper, entrepreneurs were assumed to be honest, and made the best use of the transferred resource. Yet crowdfunding markets lack the transparency, reputation building and monitoring specific to traditional finance, which can ultimately generate fraud and deception, something that our analysis did not explicitly take into account. Another limitation, in our model, investors make their decisions simultaneously. The outcome of the game is dichotomous; the project is either implemented or fails, depending on its return. In practice platforms keep a time-window of investment open and inform investors about the percentage of achievement of the investment target in real time. Thus, latecomers know how many investors have already committed to the project. Our model could be modified to a two-stage investment game, where the key decisions belong to the second stage investors.⁹ However, the investment problem of these second-period investors is not fundamentally different from the problem studied in a one-stage game.

Despite its limitations, our simple model can be seen as a first step in understanding the coordination challenge implicit in crowdfunding investing and how this strategic uncertainty affects the chances that the project is implemented. It also points out that crowdfunding is not a guarantee for financial efficiency and thus should not be seen as a natural substitute

⁹ Angeletos et al. (2007) introduced a dynamic global game with learning about the distribution of errors, which presents multiple or single equilibria depending on the amount of uncertainty.

for traditional forms of project finance. Finally, platform market power could increase these inefficiencies, which calls for increased competition in this market and a close monitoring of excessive profits by antitrust authorities.

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7 Appendix : Calculations

7.1 The equilibrium solution

Recall Equations (6) and (8):

$$[(x^* + \epsilon) - \theta^*][(x^* + \epsilon) + \theta^* - 2\rho] = 4\epsilon r$$

$$(x^* - \theta^*) = \omega + \epsilon(1 - 2v)$$

We replace $(x^* - \theta^*) = \omega + \epsilon(1 - 2v)$ in the former:

$$\begin{aligned} [\omega + 2\epsilon(1 - v)][(x^* + \epsilon) + \theta^* - 2\rho] &= 4\epsilon r \\ [(x^* + \epsilon) + \theta^* - 2\rho] &= \frac{4\epsilon r}{[\omega + 2\epsilon(1 - v)]} \\ x^* + \theta^* &= \frac{4\epsilon r}{[\omega + 2\epsilon(1 - v)]} - \epsilon + 2\rho \end{aligned}$$

Thus:

$$\begin{aligned} x^* - \theta^* &= \omega + \epsilon(1 - 2v) \\ x^* + \theta^* &= \frac{4\epsilon r}{[\omega + 2\epsilon(1 - v)]} - \epsilon + 2\rho \end{aligned}$$

The sum of the two equations leads to:

$$\begin{aligned} 2x^* &= \frac{4\epsilon r}{[\omega + 2\epsilon(1 - v)]} - \epsilon + 2\rho + \omega + \epsilon(1 - 2v) \\ x^* &= \frac{2\epsilon r}{[\omega + 2\epsilon(1 - v)]} + \rho + 0.5\omega - \epsilon v \\ \theta^* &= x^* - \omega - \epsilon(1 - 2v) \\ &= \frac{2\epsilon r}{[\omega + 2\epsilon(1 - v)]} + \rho - 0.5\omega - \epsilon(1 - v) \end{aligned}$$

7.2 The financial efficiency condition

All projects are financially efficient if:

$$\begin{aligned}
 (\theta^* - \rho) &> r \\
 \frac{2\epsilon r}{[\omega + 2\epsilon(1-v)]} + \rho - 0.5\omega - \epsilon(1-v) &> r + \rho \\
 \frac{2\epsilon r}{[\omega + 2\epsilon(1-v)]} - 0.5\omega - \epsilon(1-v) &> r \\
 \frac{4\epsilon r}{[\omega + 2\epsilon(1-v)]} - 2r &> \omega + 2\epsilon(1-v) \\
 4\epsilon r - 2r[\omega + 2\epsilon(1-v)] &> [\omega + 2\epsilon(1-v)]^2 \\
 2r[2\epsilon - \omega - 2\epsilon(1-v)] &> [\omega + 2\epsilon(1-v)]^2 \\
 2r(2\epsilon v - \omega) &> [\omega + 2\epsilon(1-v)]^2
 \end{aligned}$$

And, in the opposite case, some inefficient project can be implemented if:

$$H = [\omega + 2\epsilon(1-v)]^2 - 2r(2\epsilon v - \omega) > 0$$

The function $H = H(\omega)$ is a convex parable.

$$\begin{aligned}
 H(\omega) &= [\omega + 2\epsilon(1-v)]^2 - 2r(2\epsilon v - \omega) \\
 &= \omega^2 + 4\omega\epsilon(1-v) + 4[\epsilon(1-v)]^2 - 4r\epsilon v + 2r\omega \\
 &= \omega^2 + 2\omega[2\epsilon(1-v) + r] + 4[\epsilon(1-v)]^2 - 4r\epsilon v
 \end{aligned}$$

To determine the solutions to $H(\omega) = 0$, we calculate the (half) discriminant:

$$\begin{aligned}
\Delta &= [2\epsilon(1-v) + r]^2 - 4([\epsilon(1-v)]^2 - r\epsilon v) \\
&= [2\epsilon(1-v) + r]^2 - 4[\epsilon(1-v)]^2 + 4r\epsilon v \\
&= 4[\epsilon(1-v)]^2 + 4r\epsilon(1-v) + r^2 - 4[\epsilon(1-v)]^2 + 4r\epsilon v \\
&= 4r\epsilon(1-v) + r^2 + 4r\epsilon v \\
&= 4r\epsilon + r^2
\end{aligned}$$

The roots of $H(\omega) = 0$ are thus:

$$\omega_{1,2} = -[2\epsilon(1-v) + r] \pm \sqrt{4r\epsilon + r^2}.$$

7.3 The expected profit

$$\Pi = \rho \int_{\theta^*(\rho)}^Z l(\theta, x^*(\rho)) dF(\theta)$$

As it has been previously shown (equations 4 and 3), for any θ , the frequency of investors is given by:

$$l(\theta, x^*) = (1-\gamma)\frac{1}{2\epsilon}[\theta + \epsilon - x^*] + \gamma\frac{1}{2\epsilon}[\theta + \epsilon + \mu - x^*] = \frac{1}{2\epsilon}[\theta + \epsilon - x^* + \omega]$$

where now $x^* = x^*(\rho)$ according to equation (9).

The expected profit becomes:

$$\begin{aligned}
\Pi &= \rho \int_{\theta^*}^Z \frac{1}{2\epsilon} [\theta + \epsilon - x^* + \omega] dF(\theta) \\
&= \frac{\rho}{2Z\epsilon} [0.5\theta^2 + (\epsilon - x^* + \omega)\theta]_{\theta^*}^Z \\
&= \frac{\rho}{2Z\epsilon} [(\epsilon - x^* + \omega + 0.5Z + 0.5\theta^*)(Z - \theta^*)]
\end{aligned}$$

According to Eq. (6), we know that $(x^* - \theta^*) = \omega + \epsilon(1 - 2v)$, thus $-x^* + \omega + \epsilon = -\theta^* + 2\epsilon v$.

The expected profit becomes:

$$\Pi = \frac{\rho [0.5(Z - \theta^*) + 2\epsilon v] (Z - \theta^*)}{2Z\epsilon}$$

Our problem is defined only for $\theta^* < Z$.

Remember the equilibrium definition of θ^* in Eq. (10), $\theta^* = \frac{2\epsilon r}{[\omega + 2\epsilon(1-v)]} + \rho - 0.5\omega - \epsilon(1-v)$. We have $Z - \theta^* = Z - \frac{2\epsilon r}{[\omega + 2\epsilon(1-v)]} - \rho + 0.5\omega + \epsilon(1-v)$. Denoting by:

$$a = Z - \frac{2\epsilon r}{[\omega + 2\epsilon(1-v)]} + 0.5\omega + \epsilon(1-v) > 0$$

we obtain $(Z - \theta^*) = (a - \rho)$. The expected profit can be written as:

$$\Pi(\rho) = (2Z\epsilon)^{-1} \rho [0.5(a - \rho) + 2\epsilon v] (a - \rho).$$

This is a polynomial of the third degree.

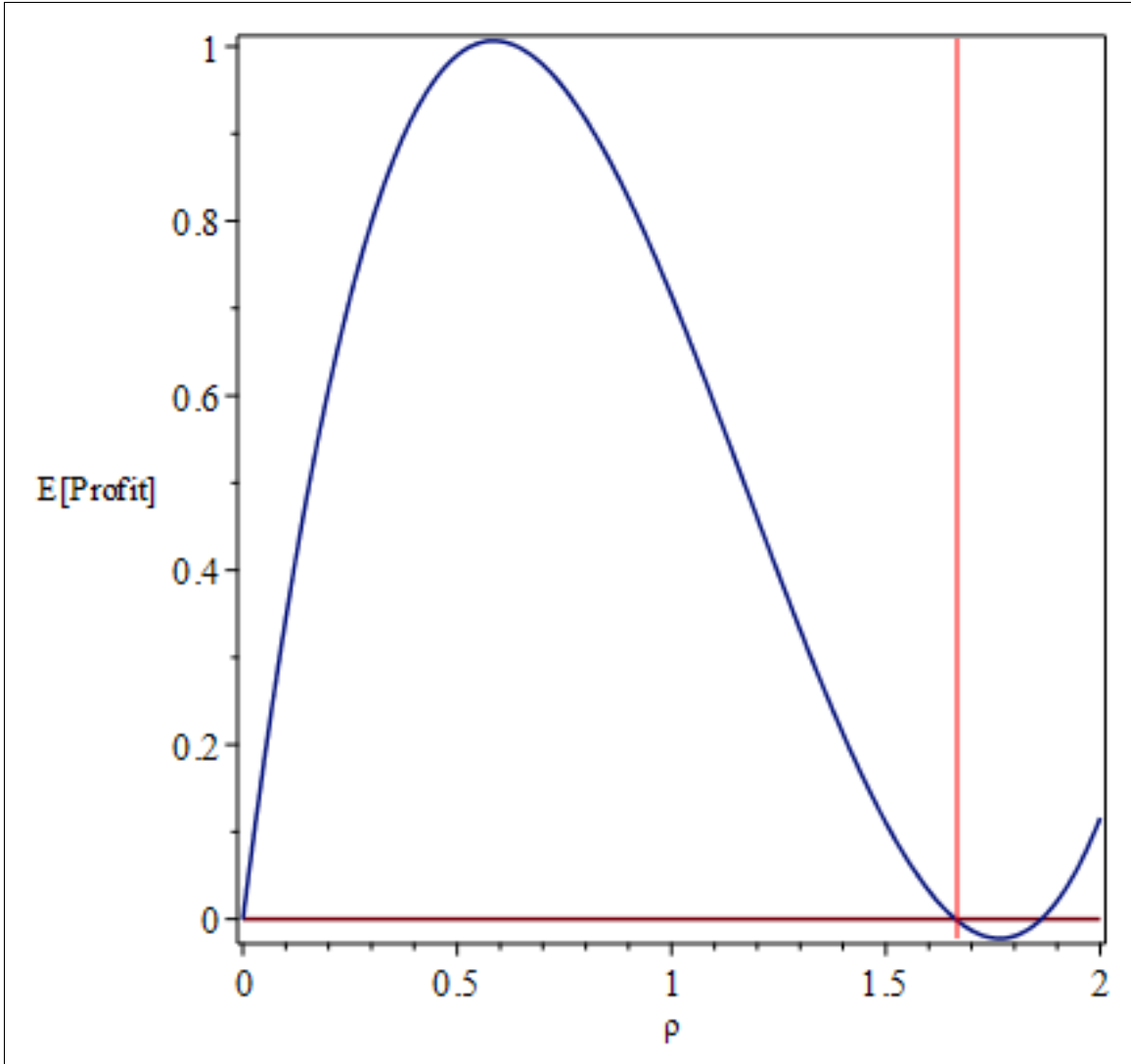
$\Pi(\rho) = 0$ has three solutions: $\rho_1 = 0$, $\rho_2 = a$, $\rho_3 = a + 4\epsilon v$, with $\rho_1 < \rho_2 < \rho_3$.

Figure 1 presents the plot of the expected profit depending on ρ . (Parameters are $Z = 2$, $\epsilon = 0.10$, $\omega = 0.025$, $v = 0.5$, $r = 0.25$):

7.4 The maximum of the expected profit

The derivative of the profit function is:

$$\begin{aligned} (2Z\epsilon) \frac{d\Pi}{d\rho} &= [0.5(a - \rho) + 2\epsilon v] (a - \rho) - 0.5\rho(a - \rho) - \rho [0.5(a - \rho) + 2\epsilon v] \\ &= 0.5(a - \rho)^2 + 2\epsilon v(a - \rho) - 0.5\rho(a - \rho) - 0.5\rho(a - \rho) - 2\rho\epsilon v \\ &= 0.5(a - \rho)^2 + 2\epsilon v(a - \rho) - \rho(a - \rho) - 2\rho\epsilon v \\ &= 0.5(a - \rho)^2 + 2\epsilon va - \rho(a - \rho) - 4\rho\epsilon v \\ &= 0.5a^2 - a\rho + 0.5\rho^2 + 2\epsilon va - \rho a + \rho^2 - 4\rho\epsilon v \\ &= 1.5\rho^2 - 2\rho(a + 2\epsilon v) + 0.5a^2 + 2\epsilon va \end{aligned}$$



It turns out that $\left[\frac{d\Pi}{d\rho}\right]_{\rho=0} > 0$.

The first order condition for profit maximization $\frac{d\Pi}{d\rho} = 0$ leads to:

$$\hat{\rho}_{1,2} = \frac{2}{3} \left[(a + 2\epsilon v) \pm \sqrt{(0.5a + 2\epsilon v)^2 - \epsilon v a} \right]$$

The first root, $\hat{\rho}_1 \in [0, \rho_2]$ corresponds to a local maximum of the profit function, the second root, $\hat{\rho}_2 \in [\rho_2, \rho_3]$ corresponds to a local minimum.

Our problem is not defined for $\rho > \rho_2$, thus the local maximum is the only maximum.

7.5 Overenthusiasm and the platform fee

Recall the definition: $a = Z - \frac{2\epsilon r}{[\omega + 2\epsilon(1-v)]} + 0.5\omega + \epsilon(1-v)$. The derivative of a with respect to ω is positive:

$$\frac{da}{d\omega} = \frac{2\epsilon r}{[\omega + 2\epsilon(1-v)]^2} + \frac{1}{2} > 0$$

Then recall the definition of the optimal tax:

$$\hat{\rho} = \frac{2}{3} \left[(a + 2\epsilon v) - \sqrt{(0.5a + 2\epsilon v)^2 - \epsilon v a} \right]$$

$$\begin{aligned} \frac{d\hat{\rho}}{d\omega} &= \frac{2}{3} \left[\frac{da}{d\omega} - \frac{1}{2} [(0.5a + 2\epsilon v)^2 - \epsilon v a]^{-1/2} [(0.5a + 2\epsilon v) - \epsilon v] \frac{da}{d\omega} \right] \\ &= \frac{2}{3} \frac{da}{d\omega} \left[1 - \frac{1}{2} [(0.5a + 2\epsilon v)^2 - \epsilon v a]^{-1/2} (0.5a + \epsilon v) \right] \end{aligned}$$

As $\frac{da}{d\omega} > 0$,

$$\begin{aligned} \frac{d\hat{\rho}}{d\omega} &> 0 \Leftrightarrow \left[1 - \frac{1}{2} [(0.5a + 2\epsilon v)^2 - \epsilon v a]^{-1/2} (0.5a + \epsilon v) \right] > 0 \\ &\Leftrightarrow 2 [(0.5a + 2\epsilon v)^2 - \epsilon v a]^{1/2} > (0.5a + \epsilon v) \\ &\Leftrightarrow 4(0.5a + 2\epsilon v)^2 - (0.5a + \epsilon v)^2 - 4\epsilon v a > 0 \\ &\Leftrightarrow ((a + 4\epsilon v) - (0.5a + \epsilon v)) ((a + 4\epsilon v) + (0.5a + \epsilon v)) - 4\epsilon v a > 0 \\ &\Leftrightarrow (0.5a + 3\epsilon v) (1.5a + 5) - 4\epsilon v a > 0 \\ &\Leftrightarrow 0.75a^2 + 2.5\epsilon v a + 4.5\epsilon v a + 15(\epsilon v)^2 - 4\epsilon v a > 0 \\ &\Leftrightarrow 0.75a^2 + 3\epsilon v a + 15(\epsilon v)^2 > 0 \\ &\Leftrightarrow a^2 + 4\epsilon v a + 20(\epsilon v)^2 > 0 \end{aligned}$$